

IR-Spectroscopy > Simple Harmonic Oscillator

Oscillation freq.

$$\omega_{\text{osc}} = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} \text{ Hz or s}^{-1} \quad \text{--- (1)}$$

$$\bar{\omega}_{\text{osc}} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} \text{ cm}^{-1} \quad \text{--- (2)}$$

$c = \text{cm s}^{-1}$ = speed of light

Vibrational energy for simple harmonic oscillator is

$$E_v = (\nu + \frac{1}{2}) \hbar \omega_{\text{osc}} \text{ Joules} \quad \text{--- (3)}$$

$$\nu = 0, 1, 2, \dots$$

where, ν is vibrational quantum number

$$\epsilon_v = \frac{E_v}{hc} \text{ cm}^{-1} : \because \text{ Divide eqn (3) by } hc$$

$$\therefore \epsilon_v = \left(\nu + \frac{1}{2}\right) \bar{\omega}_{\text{osc}} \text{ cm}^{-1} \quad \left(\because \bar{\omega}_{\text{osc}} = \frac{\omega_{\text{osc}}}{c} \right) \quad \text{--- (4)}$$

For lowest vibrational energy level

Put $v=0$, in

eqⁿ ③ becomes

$$E_0 = \frac{1}{2} h \omega_{\text{osc}} \text{ joules} \Leftarrow \underline{\underline{ZPE}}$$

eqⁿ ④ becomes

$$\varepsilon_0 = \frac{1}{2} \bar{\omega}_{\text{osc}} \text{ cm}^{-1} \Leftarrow \underline{\underline{ZPE}}$$

i.e. in Ground State, diatomic molecule can never have zero vibrational energy

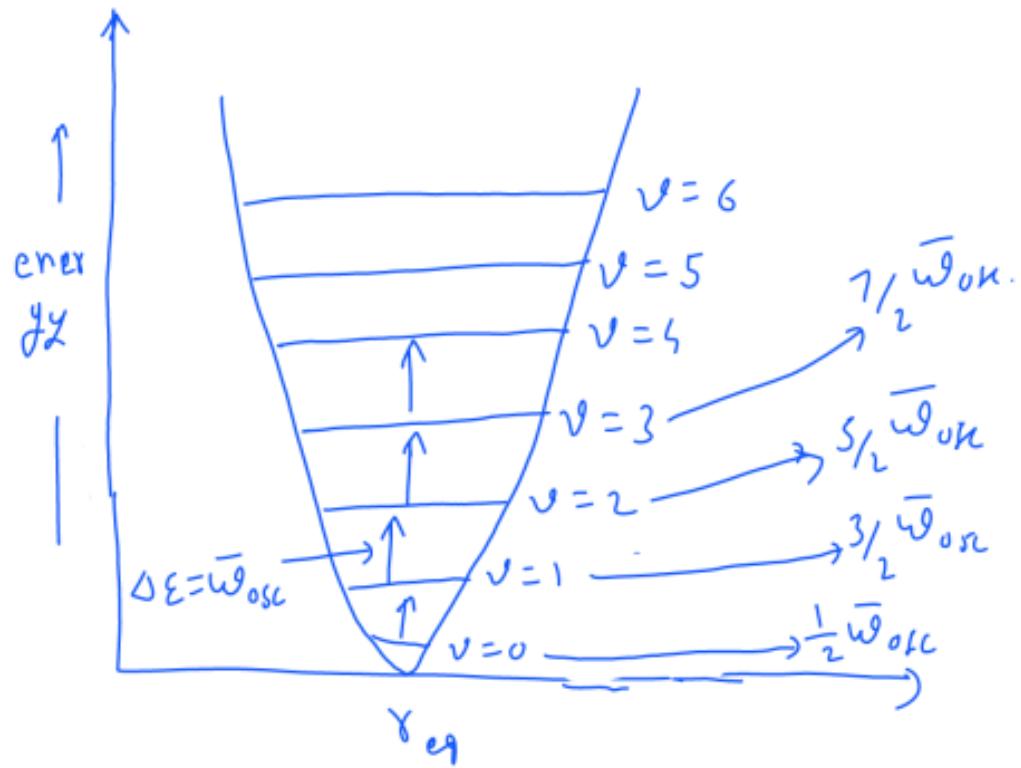
Selection rule for Harmonic Oscillator is

$$\Delta v = \pm 1$$

Condition for IR active: During vibration there must occur change in Dipole moment. i.e. heteronuclear diatomic molecules are IR active

$$\varepsilon_v = \left(v + \frac{1}{2}\right) \bar{\omega}_{\text{osc}}$$

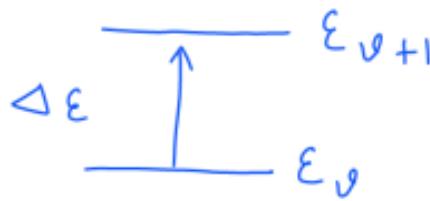
Put $v = 0, 1, 2, \dots$



Internal nuclear distance

Fig.: Vibrational energy levels and allowed transitions betw them for a diatomic molecule undergoing simple harmonic motion.

Now apply a selection rule
 ie $\Delta v = \pm 1$, ie transition takes place
 from E_v to E_{v+1} state



$$\Delta E = E_{v+1} - E_v \quad \text{from eqn ④}$$

$$\Delta E = (v+1 + \frac{1}{2}) \bar{\omega}_{osc} - (v + \frac{1}{2}) \bar{\omega}_{osc}$$

$$\Delta E = \underbrace{E_{v+1} - E_v}_{\pi} = \bar{\omega}_{osc} \text{ cm}^{-1}$$

for emission

$$\Delta E = \underbrace{E_v - E_{v+1}}_{\pi} = \bar{\omega}_{osc} \text{ cm}^{-1}$$

for absorption

ie vibrational energy levels are equally spaced

$$\therefore \bar{J}_{spectroscopic} = \Delta E = \bar{\omega}_{osc} \text{ cm}^{-1}$$